Unit \#3: Trigonometry
Topic: The Unit Circle
Objective: SWBAT find the value of a trigonometric expression by using the unit circle.

## Warm Up \#1:

Fill in the missing values in each of the charts given below:

| Function | $\frac{\pi}{6}$ | $\frac{\pi}{4}$ | $\frac{\pi}{3}$ |
| :---: | :---: | :---: | :---: |
| $\sin$ |  |  |  |
| $\cos$ |  |  |  |
| $\tan$ |  |  |  |


| Function | $\frac{\pi}{2}$ | $\pi$ | $\frac{3 \pi}{2}$ | $2 \pi$ |
| :---: | :---: | :---: | :---: | :---: |
| $\sin$ |  |  |  |  |
| $\cos$ |  |  |  |  |
| $\tan$ |  |  |  |  |

The radian measure of an angle is the arc length of the angle on the unit circle.
Relationship between radians and degrees.

| Degrees to Radians: | Radians to Degrees: |
| :--- | :--- |

A reference angle is the acute angle formed between the terminal side of a given angle and the $x$-axis.

The unit circle has a center at the origin $(0,0)$ and radius of one unit.
For any point $(x, y)$ on the circle, the lengths $x$ and $y$ become the legs of a right triangle whose hypotenuse is 1 .

| $\sin \theta=$ |
| :--- |
| $\cos \theta=$ |
| $\tan \theta=$ |
| So $(x, y)=$ |



## The unit circle is a wonderful reference tool for determining EXACT trigonometric values.



## Problem Set \#1:

Find the point $(x, y)$ on the unit circle that corresponds to the real number $t$ :

| 1) $t=\frac{5 \pi}{6}$ | 2) $t=\frac{8 \pi}{3}$ |
| :--- | :--- |
| 3) $t=-\frac{3 \pi}{4}$ | 4) $t=-\pi$ |

Find the exact value for each of the following trigonometric functions:

| 5) $\sin \frac{7 \pi}{4}=$ | 6) $\tan \frac{11 \pi}{4}=$ |
| :--- | :--- |
| 7) $\csc \frac{7 \pi}{6}=$ | 8) $\cos -\frac{5 \pi}{2}=$ |
| 11) $\sin -\frac{\pi}{6}=$ | $12) \cot \frac{5 \pi}{3}=$ |
| 13) $\cos \frac{5 \pi}{6}=$ | $14) \sec \frac{3 \pi}{4}=$ |
| 15) $\sin -\frac{4 \pi}{3}=$ | $16) \csc -\frac{2 \pi}{3}=$ |
| 17$) \sin \frac{9 \pi}{4}=$ | $18) \cos \frac{10 \pi}{3}=$ |
| 19$) \tan =-\frac{13 \pi}{6}$ | $20) \sec \frac{5 \pi}{4}=$ |

