

## Unit #2: Methods of Integration

Topic: U-Substitution with Trigonometric Identities

Objective: SWBAT find an indefinite integral of a trigonometric function by using a trigonometric identity and a u-substitution.

**Warm Up #3:**

Fill in the blanks for each of the trig identities shown below:

1) $\boxed{\phantom{000000}} = \frac{\sin\theta}{\cos\theta}$	2) $1 + \boxed{\phantom{000000}} = \csc^2\theta$
3) $\sec\theta = \frac{1}{\boxed{\phantom{000000}}}$	4) $\sin^2\theta + \cos^2\theta = \boxed{\phantom{000000}}$
5) $\boxed{\phantom{000000}} = \frac{\cos\theta}{\sin\theta}$	6) $1 + \tan^2\theta = \boxed{\phantom{000000}}$
7) $\csc\theta = \frac{1}{\boxed{\phantom{000000}}}$	8) $\boxed{\phantom{000000}} = \frac{1}{\tan\theta}$

Some integrals involving trigonometric functions can only be evaluated by using their trigonometric identities.

These allow the integrand to be written in an alternative form which may be integrated more easily.

*Example #1:* Evaluate  $\int \tan 5x dx$

*Example #2:* Evaluate  $\int \cos^3 x \, dx$

*Problem Set #3:* Evaluate each of the following.

1)  $\int \frac{dx}{\cos^2 2x}$

2)  $\int \cot 7x \, dx$

3)  $\int (\sin^2 3x + \cos^2 3x) dx$

4)  $\int \sec^4 x dx$

5)  $\int \frac{dx}{\sin^2 3x}$

6)  $\int \sin^3 2x dx$

7)  $\int \cot^2 3x dx$

8)  $\int (2 - \tan^2 x) dx$

9)  $\int \frac{4x^3}{\csc(x^4-1)} dx$

10)  $\int \frac{\cos x}{1-\cos^2 x} dx$

11)  $\int \frac{8}{\sec x} dx$

12)  $\int 2\sin^3 x dx$

**Answer Key:**

1) $\frac{1}{2}\tan 2x + C$	2) $\frac{1}{7}\ln \sin 7x  + C$	3) $x + C$
4) $\tan x + \frac{1}{3}\tan^3 x + C$	5) $-\frac{1}{3}\cot 3x + C$	6) $-\frac{1}{2}\cos 2x + \frac{1}{6}\cos^3 2x + C$
7) $-\frac{1}{3}\cot 3x - x + C$	8) $x - \tan x + C$	9) $-\cos(x^4 - 1) + C$
10) $-\frac{1}{\sin x} + C$	11) $8\sin x + C$	12) $-2\cos x + \frac{2}{3}\cos^3 x + C$